



- is greater than
- is more than



- is less than
- is fewer than



- is greater than or equal to
- is at least
- is no less than



- is less than or equal to
- is at most
- is no more than

Set Notation
{ , }

8 less than x
 $x - 8$

8 is less than x
 $8 < x$

Solve and graph the solution.

The sum of x and 3 is less than 8.

$$\{x \mid x < 5\}$$

Set-builder notation: x "such that" ...



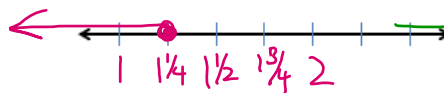
$$\begin{array}{r} x + 3 < 8 \\ -3 \quad -3 \\ \hline x < 5 \end{array}$$

Solve and graph the solution.

The difference of b and one-half is at most three-fourths.

$$\{b \mid b \leq \frac{5}{4}\}$$

Set-builder notation:



$$b - \frac{1}{2} \leq \frac{3}{4}$$

$$\begin{array}{r} b - \frac{1}{2} \leq \frac{3}{4} \\ \downarrow \\ b - \frac{2}{4} \leq \frac{3}{4} \\ +\frac{2}{4} \quad +\frac{2}{4} \end{array}$$

$$b \leq \frac{5}{4}$$

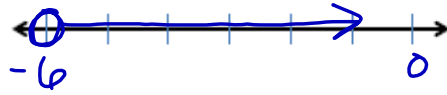
$$\begin{array}{r} 4b - 2 \leq 3 \\ +2 \quad +2 \\ \hline 4b \leq 5 \\ b \leq \frac{5}{4} \end{array}$$

Solve and graph the solution.

$$\begin{array}{r} m - 5 > -11 \\ +5 \quad +5 \\ \hline m > -6 \end{array}$$

5 subtracted from m is more than -11.

Set-builder notation: $\{m \mid m > -6\}$

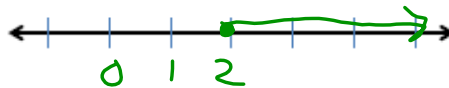


Solve and graph the solution.

$$\begin{array}{r} 10 + n \geq 12 \\ -10 \quad -10 \\ \hline n \geq 2 \end{array}$$

10 added by n is greater than or equal to 12.

Set-builder notation: $\{n \mid n \geq 2\}$



MULTIPLYING

When multiplying both sides of an inequality by a **NEGATIVE NUMBER**, the inequality symbol is reversed.

A number divided by -3 is less than 5.

One-half of a number is more than -8.

$$\begin{array}{l} \cancel{-3} \cdot \frac{n}{\cancel{-3}} < 5 \cdot \cancel{-3} \\ n > -15 \end{array}$$

$$\begin{array}{l} 2 \cdot \frac{1}{2}n > -8 \cdot 2 \\ n > -16 \end{array}$$

$\left\{ \begin{array}{l} -\frac{2}{3} \text{ of a number} \\ \text{is less than} \\ -4 \\ -\frac{2}{3}n < -4 \\ -\frac{3}{2} \cdot \frac{2}{3}n > -4 \cdot \frac{3}{2} \\ n > 6 \end{array} \right.$

DIVIDING

When dividing both sides of an inequality by a **NEGATIVE NUMBER**, the inequality symbol is reversed.

Four times a number is at least 10.

Negative five times a number is no more than -10.

$$\begin{array}{l} 4x \geq 10 \\ \frac{4x}{4} \geq \frac{10}{4} \\ x \geq \frac{5}{2} \end{array}$$

$$\begin{array}{l} -5n \leq -10 \\ \frac{-5n}{-5} \geq \frac{-10}{-5} \\ n \geq 2 \\ \{n \mid n \geq 2\} \end{array}$$

* One eighth of a number is less than or equal to 3.

$$\frac{1}{8}x \leq 3$$

$$8 \cdot \frac{1}{8}x \leq 3 \cdot 8$$

$$x \leq 24$$



A number divided by 4 is less than -2.

* Negative one-sixth of a number is less than -9.

$$-\frac{1}{6}x < -9$$

$$-6 \cdot -\frac{1}{6}x > -9 \cdot -6$$

$$x > 54$$

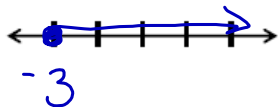


Three times a number is at least negative nine.

$$3x \geq -9$$

$$x \geq -3$$

$$\{x | x \geq -3\}$$



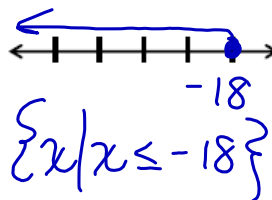
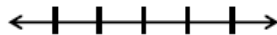
Negative twelve times a number is less than 84.

$$-12x < 84$$

Negative two-thirds times a number is at least 12.

$$-\frac{3}{2} \cdot -\frac{2}{3}x \geq 12 \cdot \frac{-3}{2}$$

$$x \leq -18$$



$$\{x | x \leq -18\}$$